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A cross-scale view of N and P limitation using a Bayesian hierarchical model

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Abstract

We propose a bivariate Bayesian hierarchical model (BBHM), which adds a perspective on a century-long subject of research, nitrogen (N) and phosphorus (P) dynamics in freshwater and coastal marine ecosystems. The BBHM is differentiated from existing approaches by modeling multiple aspects of N-P relationships-N and P concentration variability, ratio, and correlation-simultaneously, allowing these aspects to vary by seasonal and/or spatial components. The BBHM is applied to three aquatic systems, Finnish Lakes, Saginaw Bay, and the Neuse Estuary, which exhibit differing landscapes and complexity of nutrient dynamics. Our model reveals N and P dynamics that are critical to inferring unknown N and P distributions for the overall system as well as for within system variability. For Finnish lakes, strong positive within- and among-lake N and P correlations indicate that the rates of N and P biogeochemical cycles are closely coupled during summer across the different lake categories. In contrast, seasonal decoupling between N and P cycles in Saginaw Bay is evidenced by the large variability in monthly correlations and the seasonal changes in the N distribution. The results underscore the pivotal role that dreissenids have had on the cycling of nutrients and resurgence of eutrophication. The presence of clear seasonality and a spatial gradient in the distributions and N and P in the Neuse Estuary suggest that riverine N input is an important source in the season-space N dynamics, while summer sediment release is a major process regulating seasonal P distribution.

Introduction

Eutrophication mitigation is an ongoing challenge in aquatic ecosystem management. Reducing nutrient inputs remains the most viable option for eutrophication control, and management actions are generally directed toward controlling the nutrient, either nitrogen (N) or phosphorus (P), that is believed to limit primary production. The prevailing outlook since the 1970s has been that P is generally limiting in freshwater systems, while N usually limits algal growth in coastal, marine environments (Krumbein 1981; Lee and Olsen 1985; Carpenter et al. 1998; Howarth and Marino 2006, Stewards and Lowe 2010). Redfield (1958) established that the atomic ratio of N:P in oceanic phytoplankton was ~16:1 (7.2:1 mass ratio) and this value is regarded as an approximate threshold delineating N vs. P limitation in both marine and freshwater systems (Guildford and Hecky 2000). Above the Redfield ratio, a system is usually considered P limited, while below this threshold N is likely to be limiting, assuming that some other characteristic is not restricting algal production. While the Redfield ratio does not fully characterize, with high certainty, nutrient limitation across all aquatic systems, it remains an easy to quantify metric that is commonly consulted in the development of eutrophication management plans.

The strict view of P vs. N limitation is currently being reexamined (Lewis and Wurtsbaugh 2008), with arguments that joint nutrient control is appropriate for managing eutrophication in coastal, marine and inland systems (Howarth and Marino 2006; Paerl 2009; Lewis et al. 2011). These assertions have arisen as localized seasonal N limitation has been documented in Lake Erie (Chaffin et al. 2013; Chaffin and Bridgeman 2014), a freshwater system long regarded as P limited. Observations of P limitation in tropical estuaries and coastal areas (Smith 1984; Short et al. 1990) and the seasonal switching of limitation in several temperate estuaries (Myers and Iverson; 1981, Nowicki and Nixon 1985; Malone et al. 1996; Rabalais et al. 2002; Cugier et al. 2005) have also highlighted the importance of P in controlling growth in brackish/saltwater systems. Additionally, N and P co-limitation has frequently been indicated in small scale experiments (Sterner 2008). Moreover, the role of N and P stoichiometry in algal toxin

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Table 1. Summary of sample size for study sites

	Groups									
Finnish lakes	I	II	III	IV	V	VI	VII	VIII	IX	
	485	6536	388	3949	1080	1326	391	2729	2544	
Saginaw Bay	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov		
	28	59	61	62	49	27	49	44		
Neuse Estuary			Winter					Spring		
	Section1	Section2	Section3	Section4	Section5	Section1	Section2	Section3	Section4	Section5
	137	137	174	131	170	154	146	170	125	158
			Summer					Fall		
	Section1	Section2	Section3	Section4	Section5	Section1	Section2	Section3	Section4	Section5
	156	147	184	124	136	162	162	218	159	225

production has recently come under investigation (Cugier et al. 2005; Smith and Schindler 2009; Davis et al. 2010; Van de Waal et al. 2014; Yuan et al. 2014).

While it is widely recognized that N and P concentrations and the N:P ratio can differ at various spatiotemporal scales (Downing 1997; Fisher et al. 1999; Hall et al. 2005), it is common to characterize systems using point estimates or summary statistics that integrate N and P spatially and/or temporally. Scale-aggregated measures may hide important system dynamics that influence N and P, and consequently, phytoplankton productivity. Additionally, because many processes affect both N and P, their concentrations are often correlated, and evaluating them independently may be misleading. Tracking changes in the correlation structure can reveal coupling and decoupling between N and P, and provide clues about the biogeochemical processes underlying these patterns.

To reveal the differing spatiotemporal dynamics of N and P within and among systems, we adopt a Bayesian hierarchical modeling approach that jointly characterizes N and P concentrations at multiple scales simultaneously, while accounting for spatio-temporal changes in their correlations. For examples we use three well-studied aquatic systems, lakes in Finland, Saginaw Bay-Michigan, USA, and the Neuse River Estuary-North Carolina, USA, each of which are aggregated at different spatial and temporal scales, and exhibit differing patterns and processes that regulate N and P behavior.

Methods

Study sites and data description

For Finnish lakes, total N (TN) and total P (TP) concentrations were sampled from 2,289 lakes during the summer (July and August) from 1988 to 2004 (Table 1 and Fig. 1) (Malve and Qian 2006). Samples are unevenly distributed among years, types, and lakes; on average eight water quality samples were collected from each lake. Finnish lakes are classified by the Finnish Environment Institute (SYKE) into nine types based on expert assessments on lake morphology and chemistry, such as depth, surface area, and color (Table 2). According to SYKE, the selected types describe the ecological status of the lakes within each group.

Saginaw Bay is a large embayment ($\sim$2,700 km^2) on Lake Huron, located in Michigan, USA (Fig. 1). Our analysis focuses on the inner portion of the Bay, which can be characterized as shallow (mean depth $\sim$5 m), warm, and eutrophic (Stow et al. 2014). TN and TP data for the bay during the growing season (April to November) of 1999–2007 were obtained from the United States Environmental Protection Agency's online STORET database (Table 1). We used Saginaw Bay as an example to highlight the seasonality of nutrient dynamics and how the N and P behavior can provide evidence on the presence of a latent variable that is mediating these changes.

The Neuse River Estuary, on the coast of North Carolina, USA, has been described in many previous reports (Mallin et al. 1993; Borsuk et al. 2004; Alameddine et al. 2011). The estuary is shallow with a mean depth of 3.6 m, a mean width of 6.5 km, a total length of 70 km, and experiences a gradient of conditions along its length (Arhonditsis et al. 2007). The uppermost section is freshwater-dominated, with high nutrient concentrations. Nutrient concentrations tend to decrease and salinity levels increase further downstream. We examined dissolved inorganic N (DIN) and dissolved inorganic P (DIP) concentrations collected from 2000 to 2005 obtained from the ModMon program (http://www.unc.edu/ims/neuse/modmon). These data were collected every other week in all seasons at five sections across the riverine-estuarine parts of the system (Fig. 1). The division of the estuary into five sections captures the nutrient and salinity gradient within the estuary (Wool et al. 2003; Borsuk, et al. 2004; Lebo et al. 2012). Data for the Neuse were grouped temporally by season, and aggregated spatially into five segments along the freshwater-salinity gradient (Table 1).

Model development

We developed a bivariate Bayesian hierarchical model (BBHM) to highlight changes in the N:P relationship within and across scales by quantifying the variability in the concentration, ratio and correlation of N and P both at fine

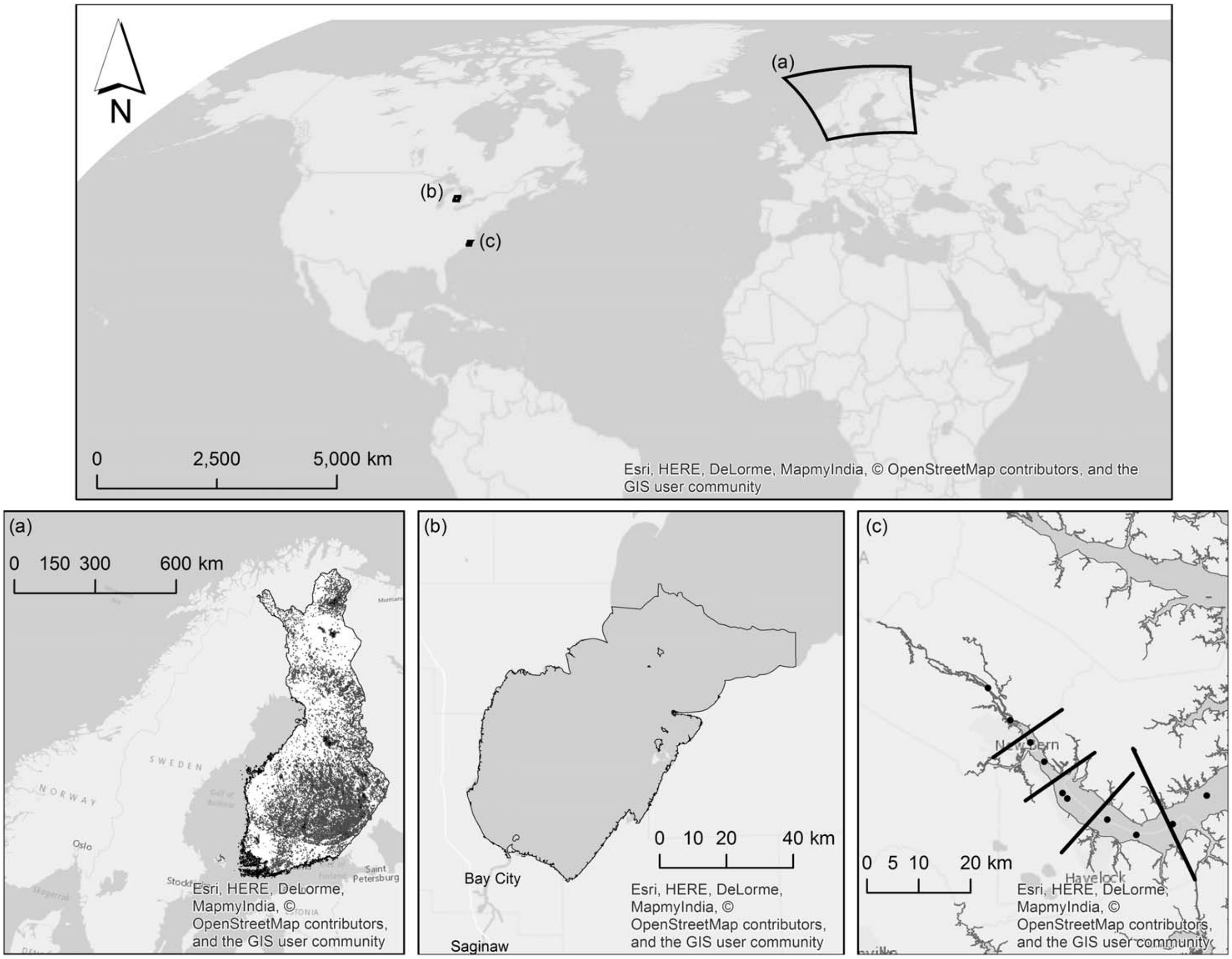

Fig. 1. (a) Finnish lakes, (b) Saginaw Bay, Lake Huron Michigan, (c) Neuse Estuary, North Carolina; also showing the monitoring stations (black circle) with respect to the five estuarine sections of the Neuse, which are delineated with black lines.

spatiotemporal scales (within a season or month, or within specific sections of a system) and at coarser scales (over multiple years, or across geographic regions). BBHMs are naturally suited for analyzing data from multiple units that are related and exhibit cross-scale structure (Qian et al. 2010; Soranno et al. 2014). They are also advantageous for estimating multiple group means, e.g., seasonal or spatial means of N and P concentrations, because they benefit from the effect of shrinking group mean estimates toward the overall mean when data are either sparse or show high variability (Qian et al. 2015). The BBHM contrasts with traditional N:P point estimates that tend to ignore the spatiotemporal correlations among sites and/or seasons, thus implicitly assuming that data from different sites/months are independent of each other. Evidence of increased estimation accuracy by pooling data from similar variables (e.g., nutrient concentrations from multiple sites) has emerged as early as the 1950s (Stein 1955). Like most water quality concentration variables, N and P concentrations are right-skewed and bounded at zero. Their univariate distributions are often approximated by a lognormal distribution (Ott 1995). We used a bivariate normal distribution to model log-transformed N and P concentrations and their correlation. N and P concentrations were simultaneously modeled at two different levels. At the individual measurement level, covarying N and P distributions were estimated for each defined group:

$$log(X_{ij}) \sim BVN(\theta_j, \Sigma_j) \tag{1}$$

The group level N and P concentrations were then linked to an overall system level N and P distribution:

Table 2. Geomorphological typology of Finnish lakes specified by Finnish Environmental Institute (SA = surface area, d = depth)

Lake Type	Name	Characteristics
I	Large, non-humic	SA>4,000 ha, color<30
II	Large, humic	SA>4,000 ha, color>30
III	Medium and small, non-humic	SA: 50-4,000 ha, color<30
IV	Medium, humic, and deep	SA: 500-4,000, color: 30-90, d>3m
V	Small, humic, and deep	SA: 50-500 ha, color: 30-90, d>3m
VI	Deep, very humic	Color>90, d>3m
VII	Shallow, non-humic	Color<30, d<3m
VIII	Shallow, humic	Color: 30-90, d<3m
IX	Shallow, very humic	Color>90, d<3m

Table 3. The prior distribution for hyper-parameters

Parameter	Distribution
σ_{N_j}	Uniform [0,4]
σ_{P_j}	Uniform [0,4]
ρ	Uniform [−1,1]
μ_N	Normal (0,100^2)
μ_P	Normal (0,100^2)
τ_N	Uniform [0,4]
τ_P	Uniform [0,4]
φ	Uniform [−1,1]

$$\theta_j \sim BVN(\mu, T) \tag{2}$$
$$\text{for } \Sigma_j = \begin{pmatrix} \sigma^2_{N_j} & \rho_j \sigma_{N_j}\sigma_{P_j} \\ \rho_j \sigma_{N_j}\sigma_{P_j} & \sigma^2_{P_j} \end{pmatrix},$$
$$\text{and } T = \begin{pmatrix} \tau^2_N & \varphi\tau_N\tau_P \\ \varphi\tau_N\tau_P & \tau^2_P \end{pmatrix},$$

where the subscript i represents an observation and j represents a group ($j = 1,\ldots,9$ for the Finnish Lakes example, representing lake types; $j = 1,\ldots,8$ for the Saginaw Bay example, representing months; $j = 1,\ldots,20$ for the Neuse River Estuary example, representing the combination of 4 seasons and 5 sections of the estuary), $X_{ij} = \begin{bmatrix} X_{N_{i,j}} \\ X_{P_{i,j}} \end{bmatrix}$ is the vector of N and P concentration measurements at sample i and group j. BVN indicates the bivariate normal distribution with the mean vector, $\theta = \begin{bmatrix} \theta_N \\ \theta_P \end{bmatrix}$, and the covariance matrix, Σ. The group mean vectors were linked by a system-level bivariate normal distribution with mean vector, $\mu = \begin{bmatrix} \mu_N \\ \mu_P \end{bmatrix}$, and covariance matrix, T. In the covariance matrices, σ and τ are standard deviations and ρ and φ are correlation coefficients. The model is a natural representation of the data structure that permits accounting for the full correlations in the data. The likelihood function of a given sample X_{ij} is thus:

$$L(\theta,\Sigma) = \frac{1}{(2\pi)^{0.5nk}|\Sigma|^{0.5n}} e^{\left(-\frac{1}{2}\sum_{i=1}^{n}(X-\theta)^T\Sigma^{-1}(X-\theta)\right)} \tag{3}$$
$$\propto \frac{1}{|\Sigma|^{0.5n}} e^{\left(-\frac{1}{2}tr\left(S\Sigma^{-1}\right)+n\left(\theta-\bar{X}\right)^T\Sigma^{-1}\left(\theta-\bar{X}\right)\right)}$$

where $\bar{X} = \frac{1}{n}\sum_{i=0}^{n} X_i$ and $S = \sum_{i=1}^{n}\left(X_i - \bar{X}\right)\left(X_i - \bar{X}\right)^T$ and tr is the trace of the matrix. Under a Bayesian framework, prior distributions need to be specified for the model parameters, $\delta = (\rho_j,\ \sigma_{N,j},\ \sigma_{P,j})$, as well as the model's hyperparameters, $\Delta = (\mu_N,\ \mu_P,\ \varphi,\ \tau_N,\ \tau_P)$. We used diffuse priors on all model parameters and hyperparameters (Table 3). A Markov chain Monte Carlo simulation method implemented in the software program WinBUGS 1.4.3 (Lunn et al. 2000) was used to simulate random samples of all model parameters from their joint posterior distributions. A model run was considered to have converged when the potential scale reduction parameter ($\hat{R}$) for all parameters was one (Gelman and Rubin 1992; Gelman and Hill 2007). Model goodness-of-fit was evaluated at the observational level by using the pivotal discrepancy measure (PDM) proposed by Yuan and Johnson (2012). The WinBUGS code for the three systems is included in the online supplementary information.

N:P ratio distributions were derived from posterior samples of N and P at appropriate scales. For example, log within-group ratios were estimated by ($\theta^m{}_{N,j}$ – $\theta^m{}_{P,j}$) and log system-wide ratio was estimated by ($\mu^m{}_N$ – $\mu^m{}_P$), where m represents the mth MCMC sample from the joint posterior distribution of all parameters. The adopted model structure reflects dependencies both between individual measurements and their corresponding group as well as across the groups and the system as a whole.

Results

Individual N and P observations were positively correlated in the Finnish Lakes and Saginaw Bay (sample correlation

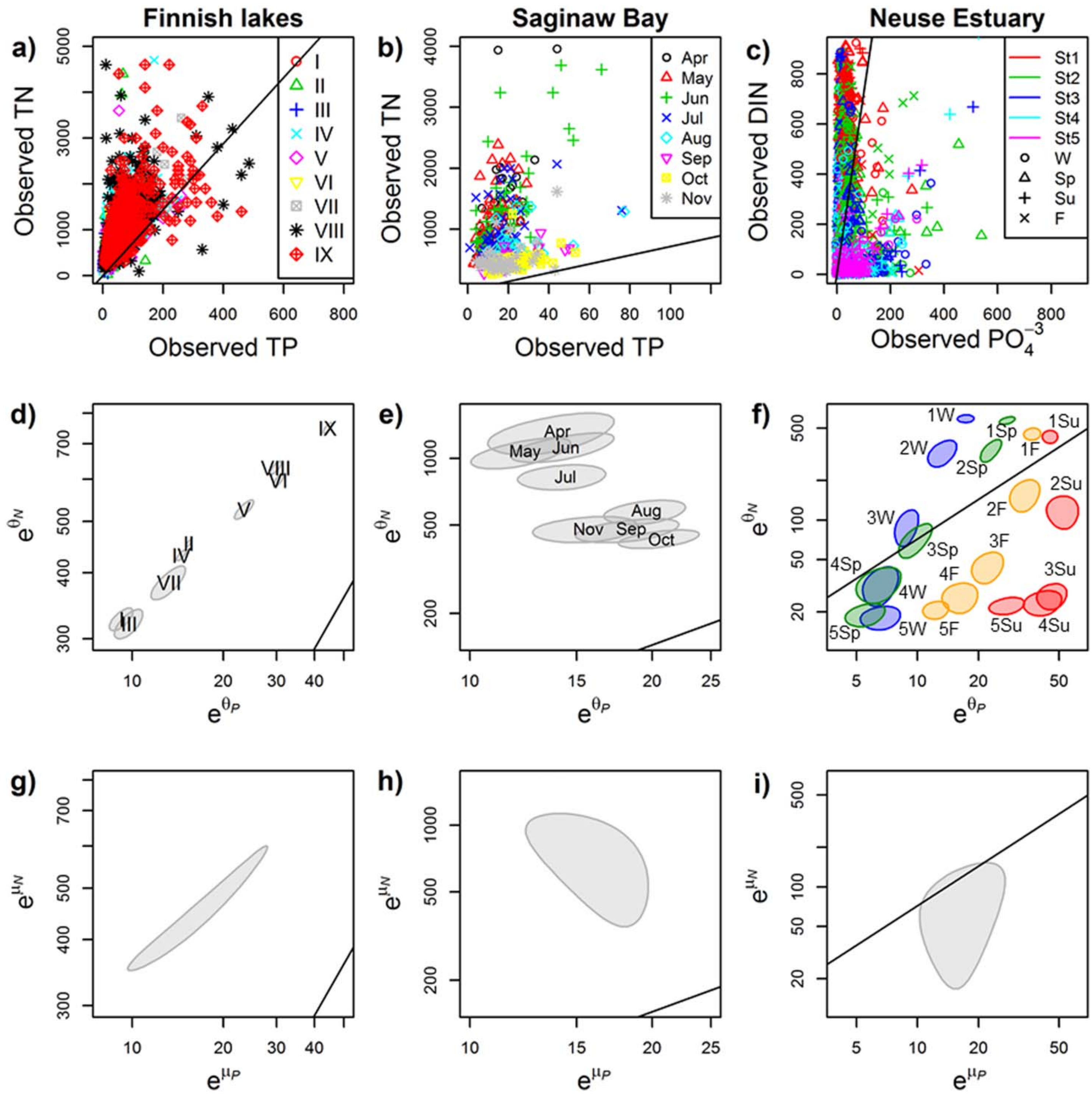

Fig. 2. Relationships between N (μg/L) and P (μg/L) concentrations for (a, d, g) Finnish lakes, (b, e, h) Saginaw Bay, and (c, f, i) the Neuse Estuary. In panels (a-c) color-symbol combinations, marked differently by group, denote individual observations. In panels (d-f) ellipses denote the 95% contour of joint distribution of group N and P from the BHBM. In panels (g-i) ellipses denote the 95% contour of joint distribution of overall system N and P from the BHBM. In all panels, solid diagonal lines indicate the Redfield ratio (mass N:P = 7.2:1). In panels f), abbreviations are the combination of section and season: the number indicates the sections 1-5 and the text indicates the season (W: Winter, Sp: Spring, Su: Summer, and F: Fall).

coefficients $r = 0.62$ and 0.41, respectively) while there was little correlation in the Neuse Estuary ($r = 0.05$) at this scale (Fig. 2a–c). Observations in the Finnish lakes are generally above the Redfield ratio as are the median values for each lake group (Fig. 2a). In Saginaw Bay all observations and monthly medians exceed the Redfield ratio (Fig. 2b). In

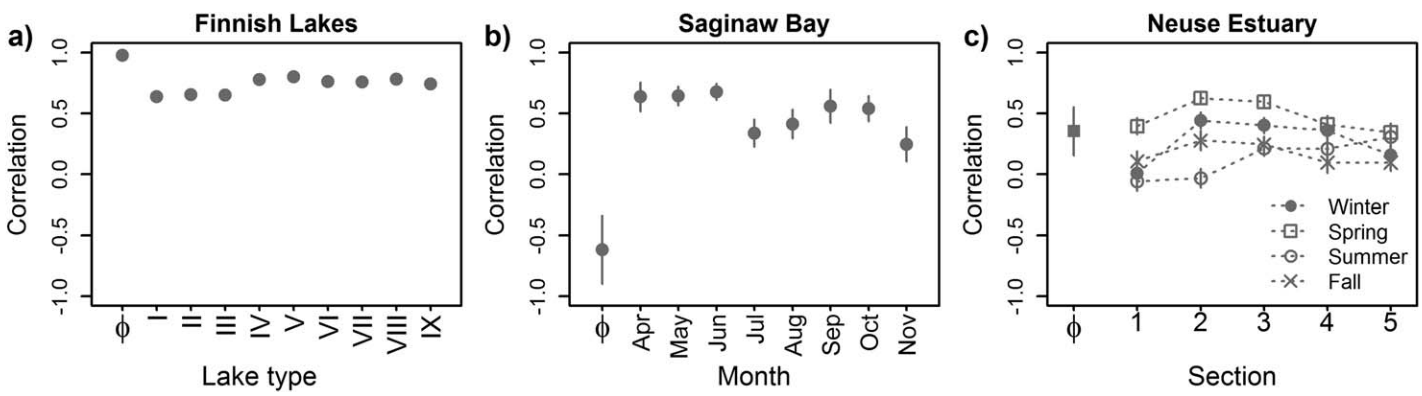

Fig. 3. Across-group (φ) and within-group (ρ) correlation between N and P for (a) Finnish lakes and (b) Saginaw Bay, and (c) the Neuse Estuary. Gray symbol and gray vertical line denote the mean and 95% interval estimated using the Bayesian hierarchical model.

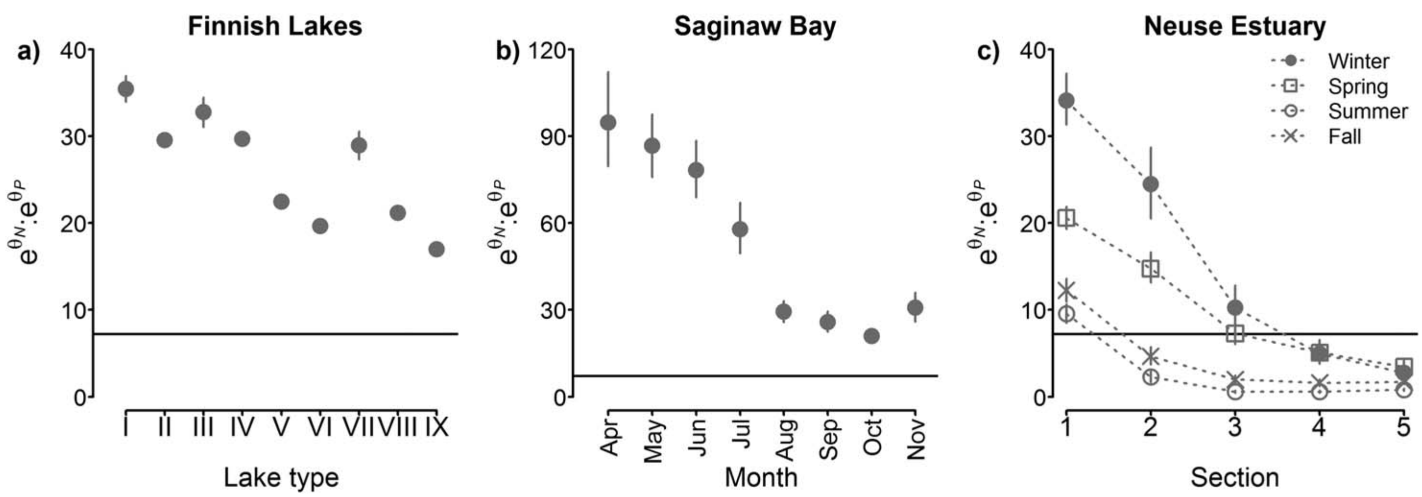

Fig. 4. Group N:P distribution for (a) Finnish lakes, (b) Saginaw Bay, and (c) Neuse Estuary. Gray circle and gray vertical line denote the median and 95% interval estimated using the Bayesian hierarchical model. Solid horizontal line indicates the Redfield ratio (mass N:P = 7.2:1).

contrast, observations and group medians straddle the Redfield ratio in the Neuse (Fig. 2c).

N:P ratios (estimated by $e^{\theta_N} : e^{\theta_P}$) show differing within group structure for each of the study sites (Fig. 2d–f). The Finnish lakes exhibit a consistent strong positive correlation between N and P within each group (Fig. 3a). All groups are well above the Redfield ratio (Figs. 2d and 4a), with ratios ranging from 17:1 to > 30:1 across lake types (Fig. 4a). Consistent with the within lake-type N and P correlation, the Finnish lake system as a whole shows a strong positive correlation that approached one. In contrast, while the within-group correlations are all positive in Saginaw Bay, the strength of correlation differs seasonally (Fig. 3b); correlations are strongest in the spring and early summer and weaken over the summer. N:P ratios are also observed to progress toward the Redfield ratio as summer progresses (Figs. 2e and 4b).

The Neuse, which was grouped spatially and temporally, exhibits a more complex pattern than the other two sites. The Neuse exhibited more differentiation in the N:P correlation. For each of the five estuarine segments, it was highest in the spring, with a decline through summer and fall, followed by a rise in the winter (Fig. 3c). Groups in the Neuse spanned the Redfield ratio (Fig. 2f), the N:P ratio generally decreased moving from upstream to downstream and from fresher to more saline conditions (Figs. 2f and 4c).Yet, across all locations there was a general seasonal progression in N:P ratios. Highest ratios were observed in winter and spring, lower ratios were found in the summer, after which the ratio subsequently increased in the fall (Figs. 2f and 4c). Interestingly, both ratios and correlations followed the same temporal pattern.

System-wide N:P ratios (estimated by $e^{\mu_N} : e^{\mu_P}$) summarize overall across-group structure (Fig. 2g–i). The N:P correlation across groups (φ) in the Finnish lakes was found to be strongly positive (very close to one) (Figs. 2g and 3a). Moreover, the overall N:P ratio for the entire system of lakes was well above the Redfield ratio (Fig. 2g). The temporally based grouping in Saginaw Bay showed a negative across-months N:P correlation (Figs. 2h and 3b), but overall the Bay was above the Redfield ratio (Fig. 2h). In the Neuse, across group correlation was positive (Figs. 2i and 3c) and overall the system was below the Redfield ratio, though the system as a whole had a small probability of exceeding it (Fig. 2i).

Discussion

Our results illustrate the utility of the BBHM to reveal N and P patterns that are not well captured by point estimates and summary statistics. This is accomplished by accounting for the covarying nature of N and P along with their variability over the time-space scales of interest. The model enables us to summarize the wide observed range of water column N and P concentrations and ratios (Fig. 2), as well as characterize their spatio-temporal variation.

The model captures multiple aspects of the N-P relationship-N and P concentration variability and correlation-simultaneously, through which N:P ratio distribution can also be characterized. Putting all the pieces together is important in assessing N and P dynamics because both the ratios and concentrations are indicative of trophic state and influence algal biomass and community composition (Smith 1982; Hecky and Kilham 1988; Smith and Bennett 1999; Guildford and Hecky 2000; Howarth and Marino 2006).

The correlation between N and P concentrations has seldom come to the forefront, in contrast to the ratio, despite the fact that the correlation carries a signal of coupling between N and P cycles along the time of year through space. Strong, positive within- and across-group correlations for the Finnish lakes (Fig. 4a) may indicate that the rates of N and P biogeochemical cycles in the summer are similar to each other both by lake-type and at the whole system-scale, albeit with different levels of P limitations. This strong coupling may mislead nutrient management decisions aiming to reduce eutrophication, particularly when N:P ratios are not consulted. The spatial distribution of N and P in Finnish lakes suggests that lake color, an indicator of dissolved carbon and humic acids, appears to be a better predictor of trophic state as compared to lake size or depth. Humic lakes appear to consistently have higher nutrient concentrations and lower N:P ratios as compared to non-humic lakes, irrespective of area and/or depth. Color levels tended to be related with N and P levels (Table 2, Fig. 2d). These relationships among the color, N and P levels were confirmed in 600 freshwater lake systems (Nürnberg and Shaw 1998).

In Saginaw Bay, a negative across-month correlation was found, which contrasts with the positive correlations observed within each month (Fig. 4b). This apparent inconsistency is an illustration of Simpson's paradox (Simpson 1951) that arises from partitioning data into subpopulations. This apparent inconsistency suggests differing drivers at shorter vs. longer time-scales. The negative across-month pattern arises as monthly P concentrations generally increase from spring through fall, while monthly N concentrations generally decrease (Fig. 3e). Interestingly, data from 1974 indicated spring peaks for both P and N concentrations (Bierman and Dolan 1981), and Stow et al (2014) reported an apparent shift in the phosphorus peak following the early 1990s dreissenid mussel invasion. The negative correlation across months may reveal a decoupling of the seasonal N and P concentration drivers which results from differing mussel filtration rates through the year. Spring tributary inputs likely consist of a high proportion of dissolved N, which is not removed via mussel filtration, and a high proportion of particulate P, which is removed by the mussels. As N and P tributary inputs decrease into the summer, so does the mussel filtration rate (Nalepa and Fahnenstiel 1995, Vanderploeg et al. 2009), favoring a relative increase in P concentrations in the bay, while N concentrations respond primarily to the declining tributary load. Thus, while tributary inputs are a common driver for N and P, at longer timescales differential internal processing causes divergent behavior in their concentrations. Failing to understand or resolve the paradoxical association between N and P at different scales can often lead to unsuitable nutrient management plans.

The Neuse River Estuary exhibits a wide variation in within-group N:P correlation (Fig. 3c). The correlation is highest in the spring and at the upstream stations, probably reflecting spring precipitation and associated watershed inputs as the main driver of N and P concentrations. Moving downstream, and during lower flow conditions, internal processes, which differentially influence N and P concentrations appear to dominate resulting in a decoupling of N and P. N concentrations in the Neuse Estuary exhibit clear spatial gradients and distinguishable seasonality (Fig. 3c). High winter-spring N concentrations followed by low summer-fall N, combined with the high upstream to low estuarine N gradient, suggest that riverine input, over internal processing, is a dominant factor in season-space N dynamics in the estuary. Like most temperate estuaries, the lower saline sections of the Neuse Estuary show strong nitrogen limitations, highlighting the importance of oceanic inputs and the lack of significant planktonic N fixation (Howarth 1988; Vitousek and Howarth 1991; Nixon 1995; Howarth and Marino 2006). Conversely, summer P peaks may imply that sediment release associated with bottom-water anoxia is an important process influencing water column P concentrations during summer (Paerl et al. 1998; Alameddine et al. 2011).

Although the Finnish lakes, Saginaw Bay, and the Neuse River Estuary reveal a mesotrophic state at the system scale (Fig. 2), variability of N and P concentrations among season or space was substantial (Fig. 3), as was the variability of the N:P ratios (Fig. 4). Given environmental heterogeneity and uncertainty, nutrient limitation of primary producers should not be determined by any single N:P ratio. Rather, N:P ratios characterize imbalances between N and P, and noticeable deviation from the Redfield ratio may be indicative of a high likelihood of N or P nutrient limitation (Hecky and Kilham 1988). Moreover, spatio-temporal shifts in the N:P ratios are often a sign of a decoupling in the nutrient cycles. In Saginaw Bay, monthly N:P ratios were all higher than the Redfield ratio, despite clear seasonality, exhibiting a tendency of continuing P limitation throughout the growing season (Figs. 2e, 4b). In the Neuse Estuary, on the other hand, complex season-space N:P patterns indicate a shifting limitation between N and P with changes in season and space (Figs. 2f, 4c).

The future application of the BBHM to other aquatic systems, which are also likely to exhibit systematic spatiotemporal differences in N and P concentrations and ratios, will enable us to characterize the nutrient limitation shift linked to specific conditions or points along a continuum of time and space. The model results highlight the need for future management-oriented load-response eutrophication models to embrace a cross-scale view of nutrient limitation. Thus, future research should link this model to biological components, such as phytoplankton abundance, or toxin concentrations, so that relevant eutrophication ecosystem response indicators are probabilistically predicted as a function of covarying N and P, while also accounting for temporal and spatial dimensions.

The fundamental eutrophication management question of whether to use single or dual nutrient control strategies is the subject of much debate in the environmental and ecological science community. Our results, suggest that differing perspectives on this question may arise depending on the scale at which the system is viewed. N and P distributions on an entire system-scale distinct from those on a group-scale necessitate the science and management community to consider the mechanisms that affect eutrophication patterns on the scale of interest. Atmospheric deposition, climate and watershed characteristics such as land-use should be accentuated on the system-scale, whereas the role of riverine nutrient input and internal processes such as sedimentation, recycling, grazing or nitrification-denitrification may be critical in determining seasonal or spatial variability in N and P dynamics.

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Conflict of Interest

None declared.

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